Univ. of Illinois Due: Wed Sept. 5, 2018 Prof. Allen

**Topics of this homework:** Basic Acoustics and units, dB, Intensity calculations, the Helmholtz resonator

## 1. The speed of sound:

- (a) What is the formula for the speed of sound?
- (b) Identify the variables: Names, units, and values of consonants.
- (c) What is the meaning of  $\eta P_0$ ?
- (d) Does  $P_0$  depend on temperature? Explain?
- (e) Does  $\rho_0$  depend on temperature or  $P_0$ ? Explain.
- (f) What is the form of the dependence of the speed of sound on temperature? Namely give the formula for c(T), and explain the dependence.

## 2. Basic equations of sound propagation:

- (a) Write out the 2x2 matrix equation that describes the propagation of 1 dimensional sound waves in a tube having area A:
- (b) Rewrite these equations as a second order equation in terms of the pressure P, and thereby find the formula for the speed of sound in terms of Z and Y:
- 3. Assume that a flash bulb puts out 50 Joules when it is triggered, and it lasts for 20  $\mu$ s. How much power is delivered while the flash is present, assuming the illumination is constant during the interval?
- 4. What is the displacement magnitude (RMS) of air particle in pm, of a pure-tone plane wave, having a pressure of 0 dB-SPL at 1 kHz.
- 5. Compare and discuss this movement with respect to the radius of a single Hydrogen atom.
- 6. A person is speaking at an intensity of  $I_0$  66 dB-SPL, as measured with a sound level meter at 1 meter.
  - (a) Find the total power in the voice assuming that the level is uniform around the head.
  - (b) Find the total power assuming that the intensity varies as

$$I(\theta, \phi) = I_0 \cos(\theta/2) \cos(\phi/2) \tag{1}$$

where  $\theta$  is the angle in the horizontal plane and  $\phi$  in the vertical plane. where  $\theta = 0, \phi = 0$  corresponds to "straight ahead."

## 7. Bels

- (a) How many millibels [mB] in 1 bel [B]?
- (b) Give the formula for the intensity in mB units.
- (c) Give the formula for the sound pressure level in cB (centibel) units.
- 8. Demonstrate that  $P_{ref} \equiv 20 \ \mu \text{Pa}$  is the same as  $I_{ref} \equiv 10^{-12} \ [\text{W/m}^2]$ .

- 9. A bottle has a neck diameter of 1 [cm] and is l=1 cm long. It is connected to the body of the bottle "barrel" which is 5 cm in diameter and L=10 cm long. Treat the barrel as a short piece of transmission line, closed at one end, which looks like a compliance  $C=V_{barrel}/\eta P_0$ , and the neck which look like a mass  $M=\rho_0 l/A_{neck}$ . These two impedances are in series, since they both see the same volume velocity (flow).
  - (a) Find the resonant frequency of the bottle. Hint: set the impedance to zero and solve for the resonant frequency in terms of M and C.
  - (b) write out the formula for the resonant frequency in terms of the dimensions of the bottle.
  - (c) calculate the resonant frequency in Hz for the dimensions given.
  - (d) Blow into a blottle and measure the resonant frequency by recording the tone, and taking the FFT of the resulting waveform, and finding the frequency (Extra credit).